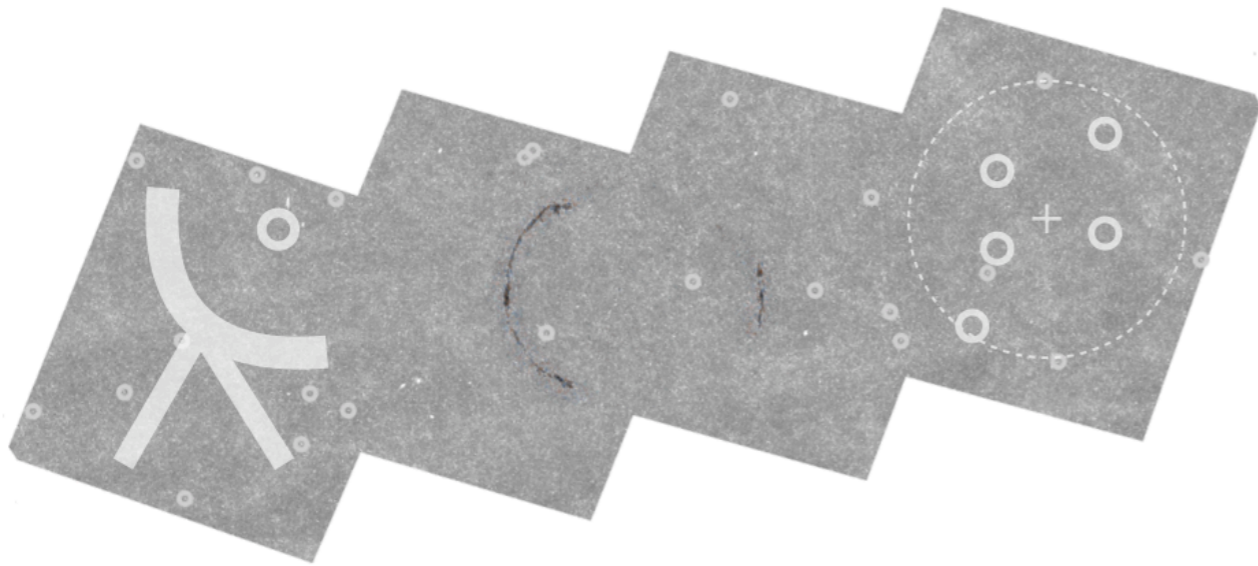


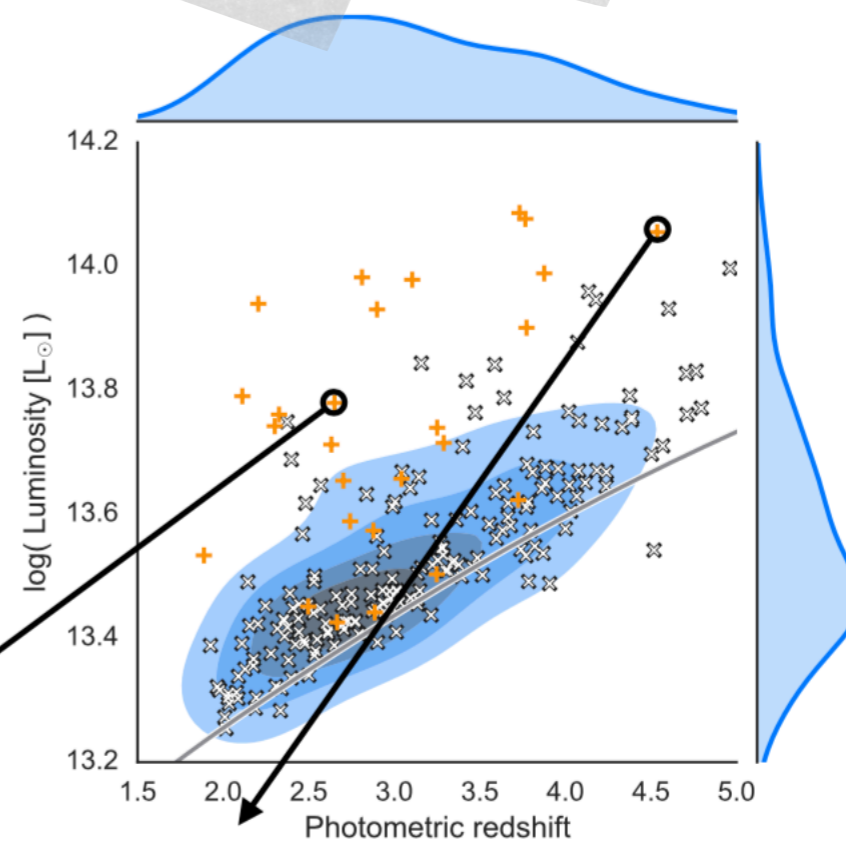
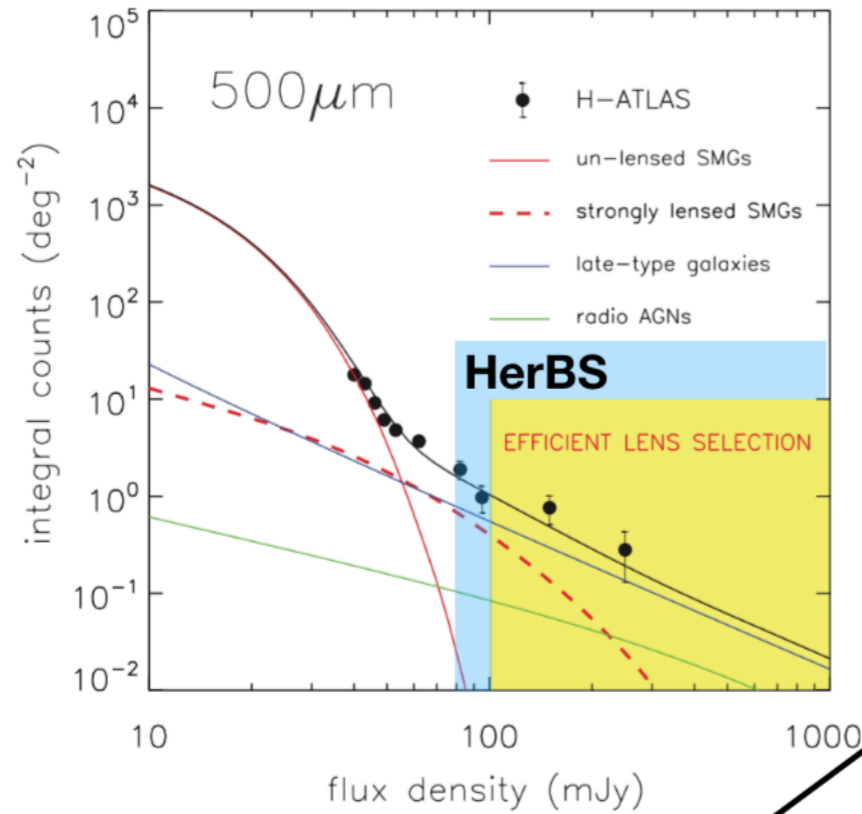
How many gravitational lenses did Herschel detect?

*Optical and near-infrared counterparts
to sub-mm sources*

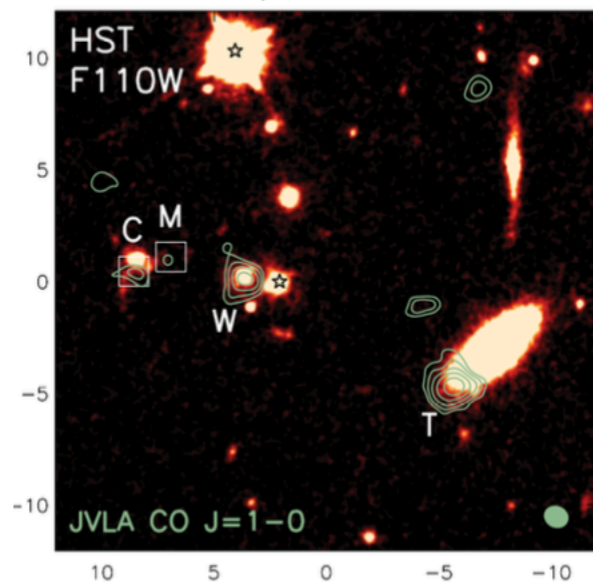


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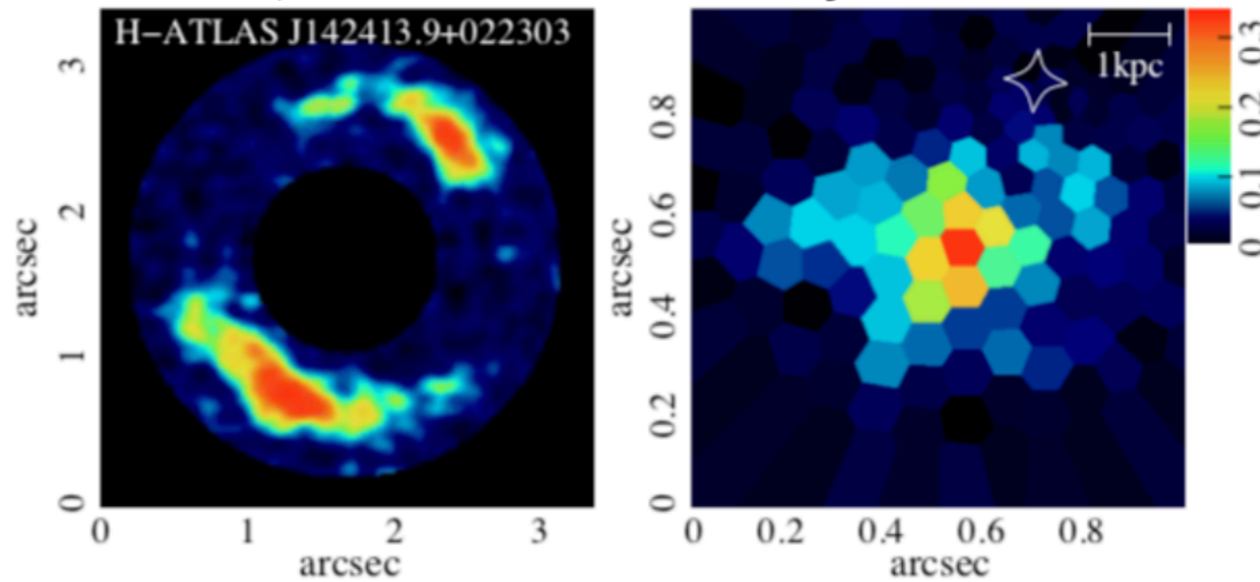
Brightest sub-mm sources are mostly lensed



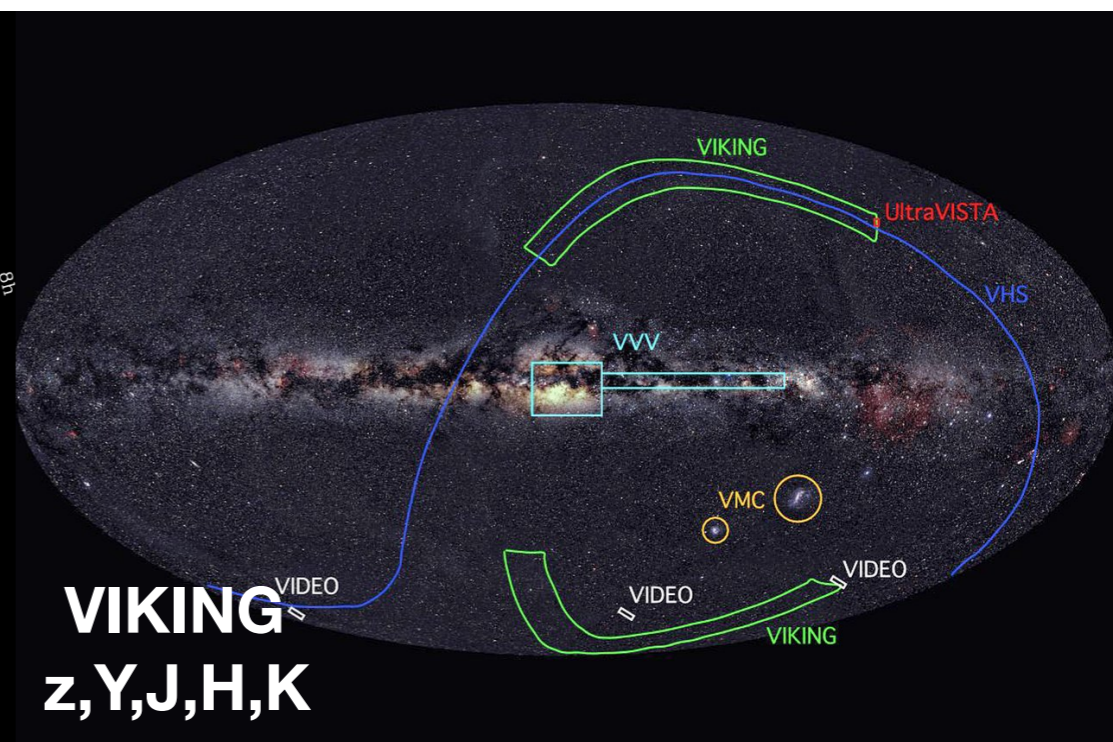
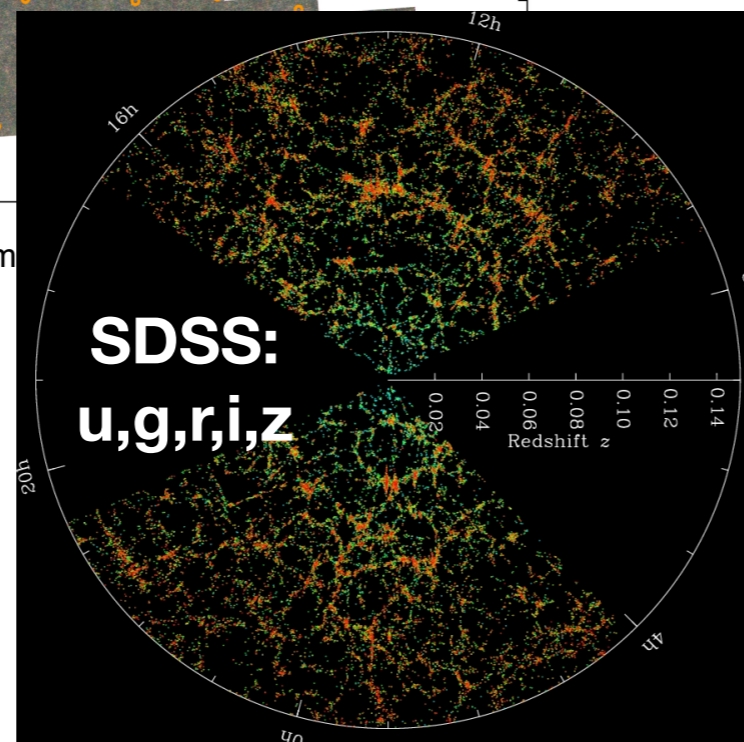
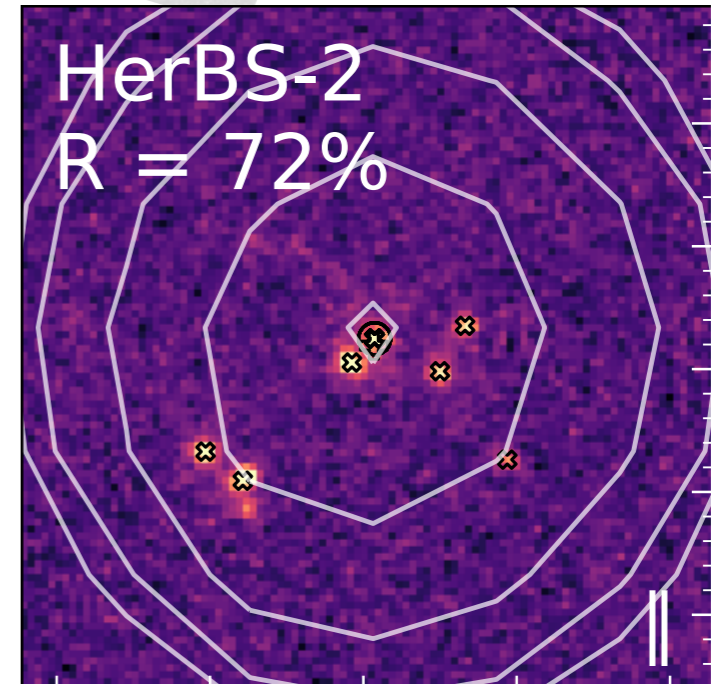
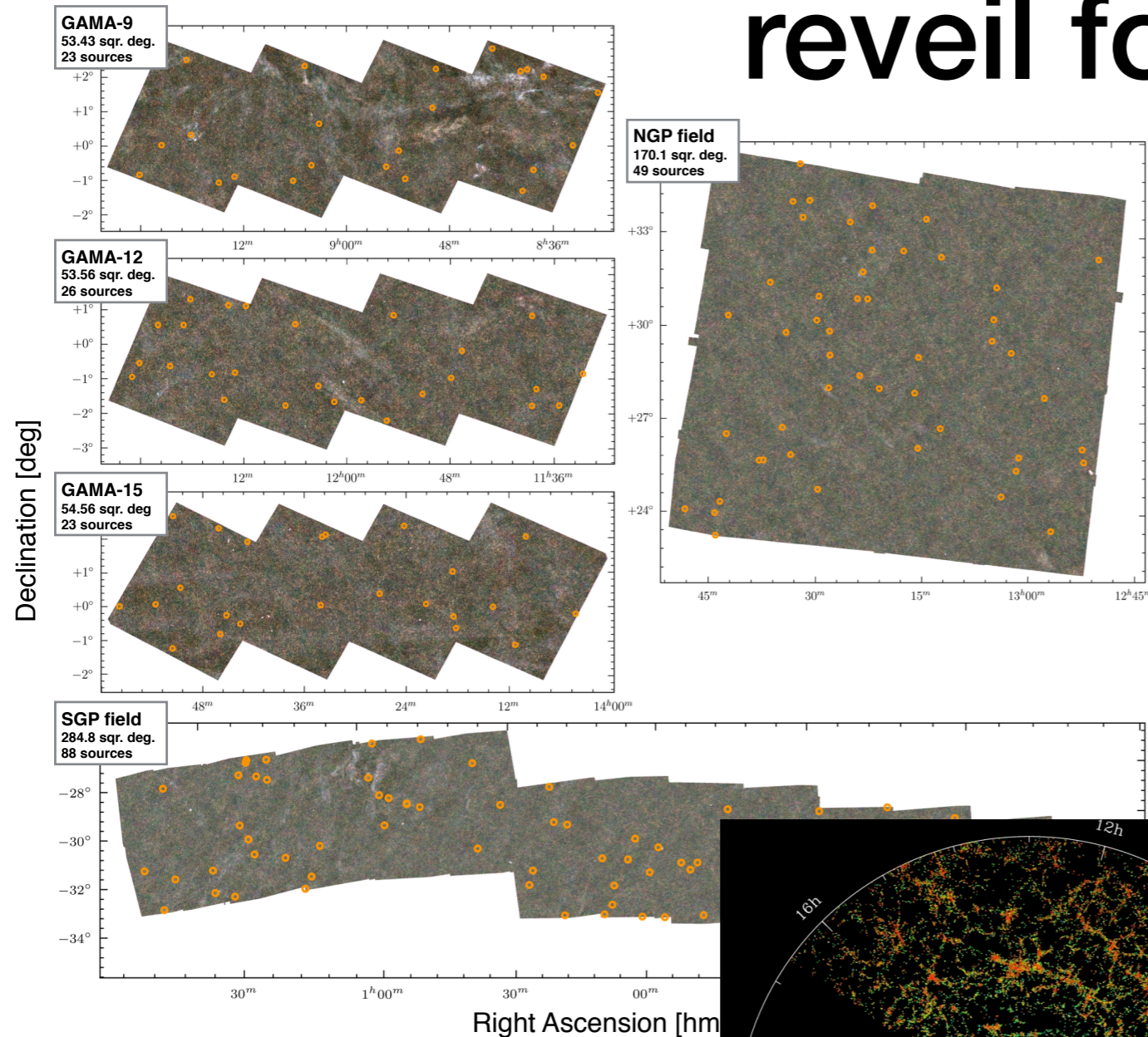
HerBS-8; Ivison et al. 2013



HerBS-13; one of the sources of Dye et al. 2018



Counterparts in SDSS and VIKING reveal foreground lenses




The probability follows from two 'simple' equations

$$L = \frac{q(m)f(r)}{n(m)} \cdot \equiv \frac{\text{Chance of source (m) at distance (r)}}{\text{Chance of a random source (m)}}$$

$$R_j = \frac{L_j}{\sum_i L_i + (1 - Q_0)} \cdot \equiv \text{Probability of this source j being a genuine counterpart}$$

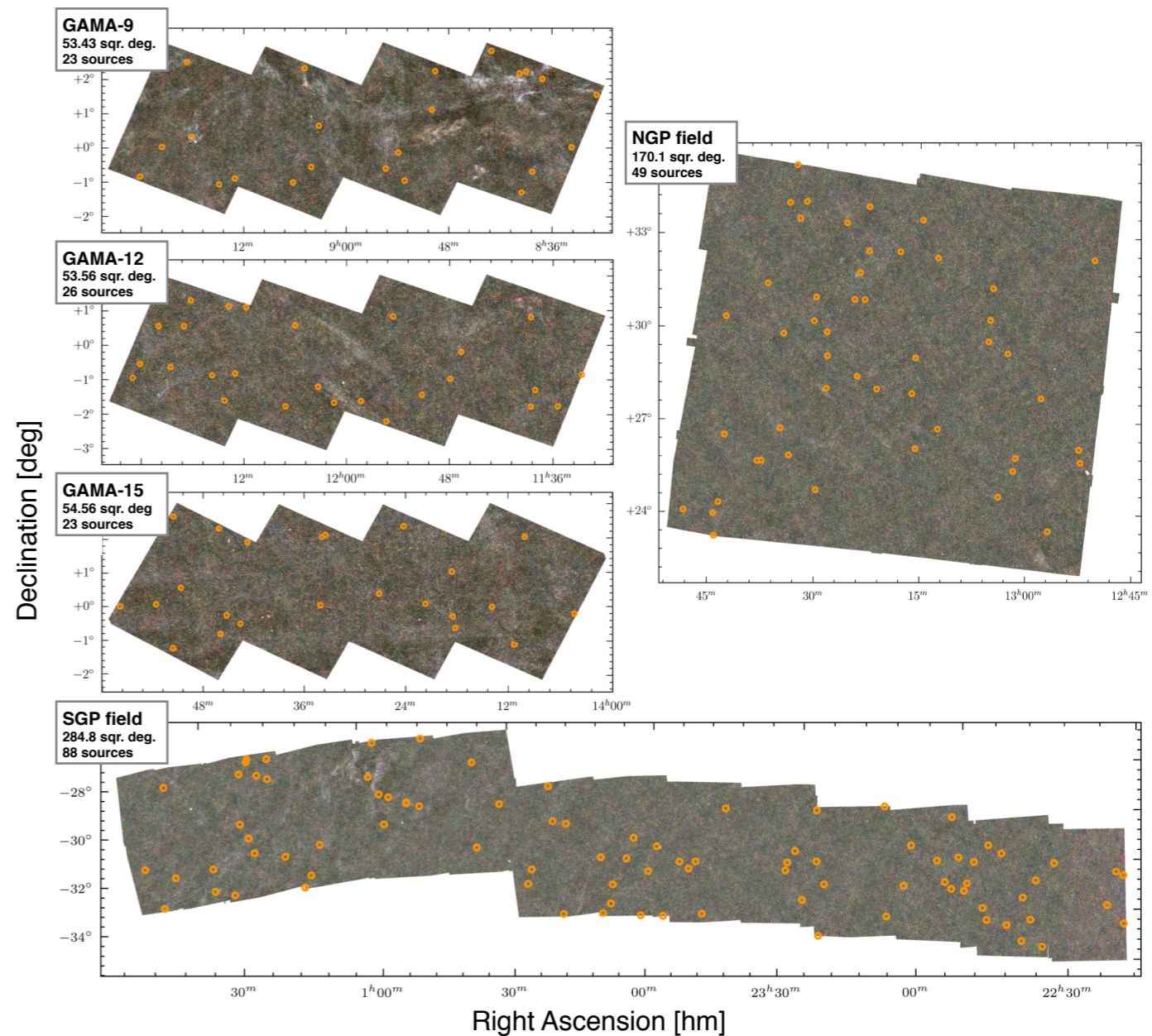
Chance the source outside of survey depth



SDSS counterparts already exist, but finds only 35% of counterparts

Table 1. The SDSS reliabilities of Herschel sources.

R	< 0.8	> 0.8	All
GAMA	52	20	72
NGP	38	11	49
Total	90	31	121




The probability follows from two 'simple' equations

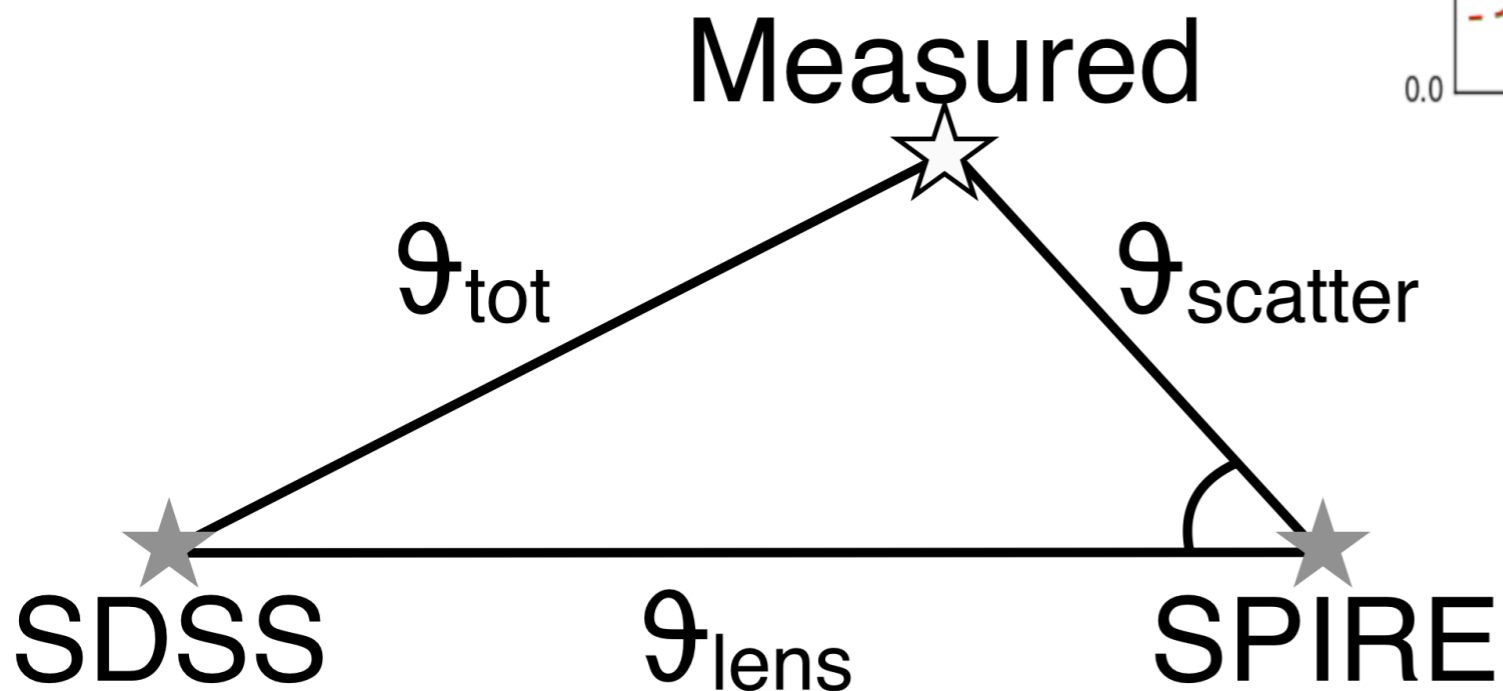
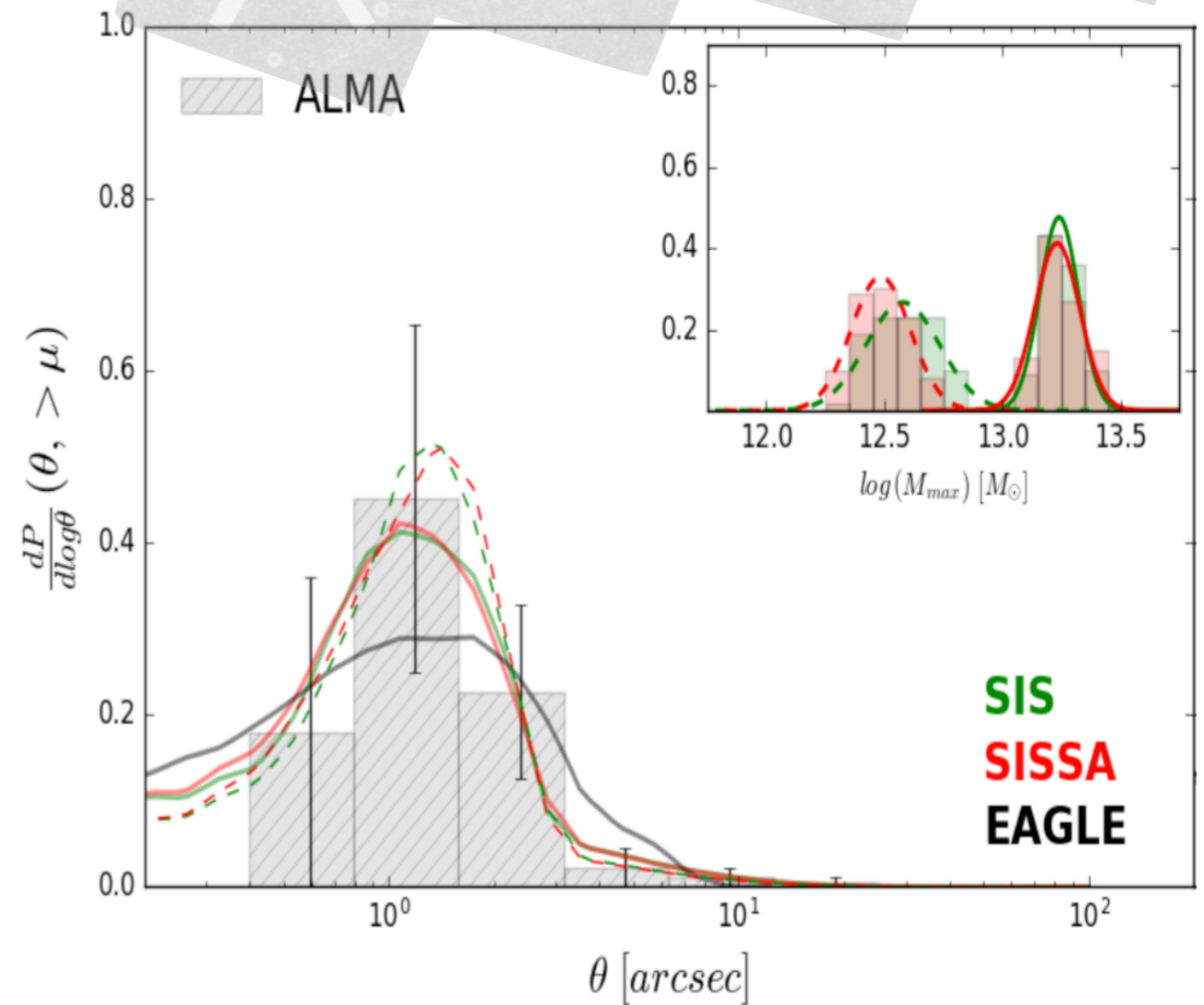
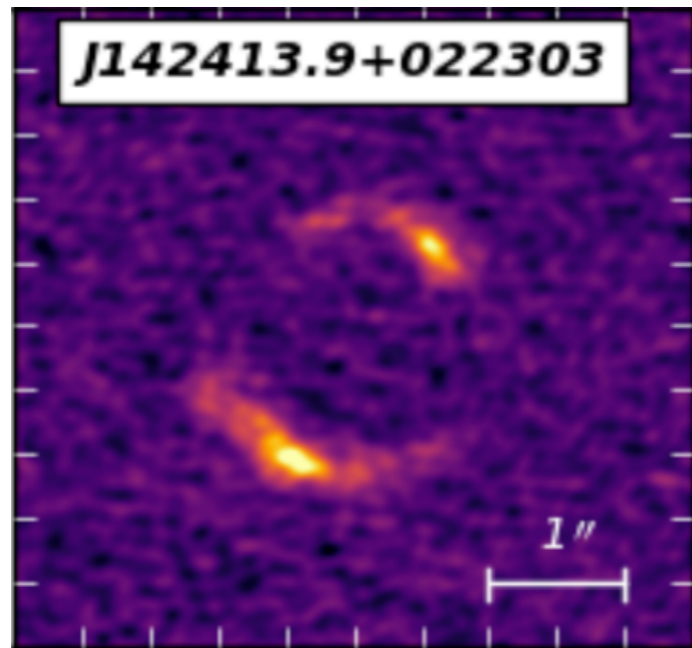
$$L = \frac{q(m) f(r)}{n(m)} \cdot \equiv \frac{\text{Chance of source (m) at distance (r)}}{\text{Chance of a random source (m)}}$$

$$R_j = \frac{L_j}{\sum_i L_i + (1 - Q_0)} \cdot \equiv \text{Probability of this source j being a genuine counterpart}$$

Chance the source outside of survey depth



Recalculating the angular probability distribution allows us to find more lenses

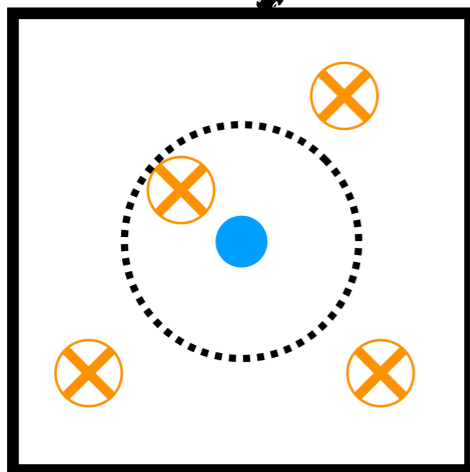


The re-analysis suggests we are missing multiple lensed sources

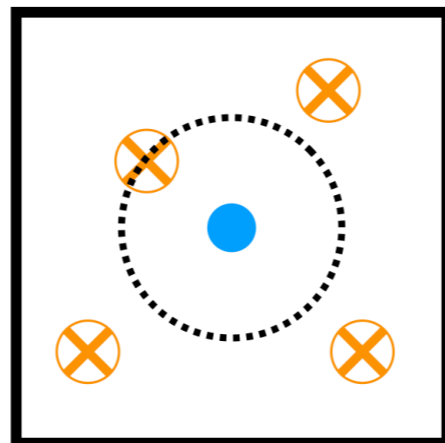
Model	Method 1	Method 2
No lens	31	31
Total model	32.5	41

**Complete
recalculation**

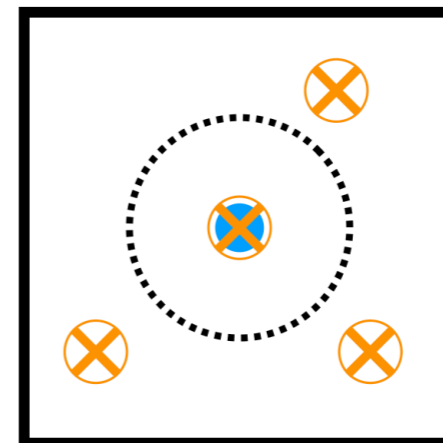
**Statistics
on reliable
sources**



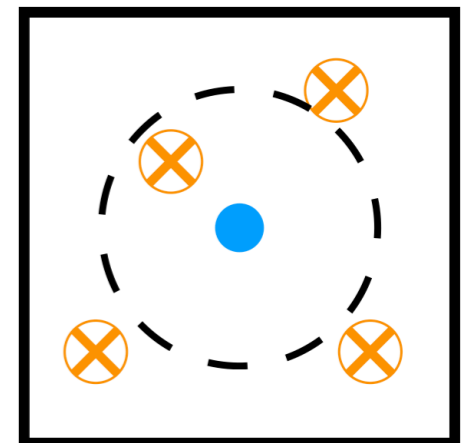
$$L \sim e^{-\theta_{sc}^2/2}$$



$$L_0$$



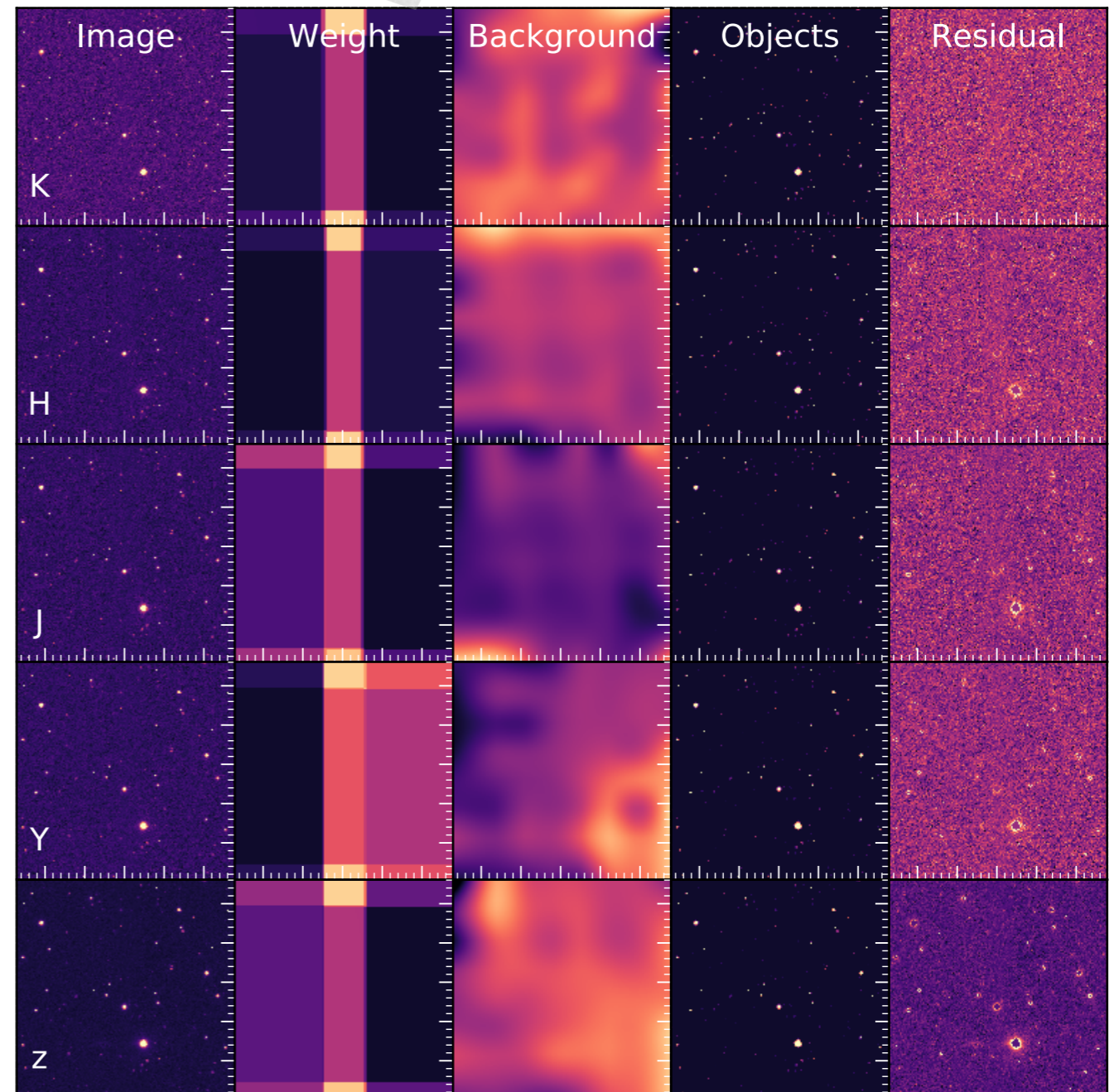
$$L' \sim f(\theta_{\text{lens}}, \theta_{sc})$$



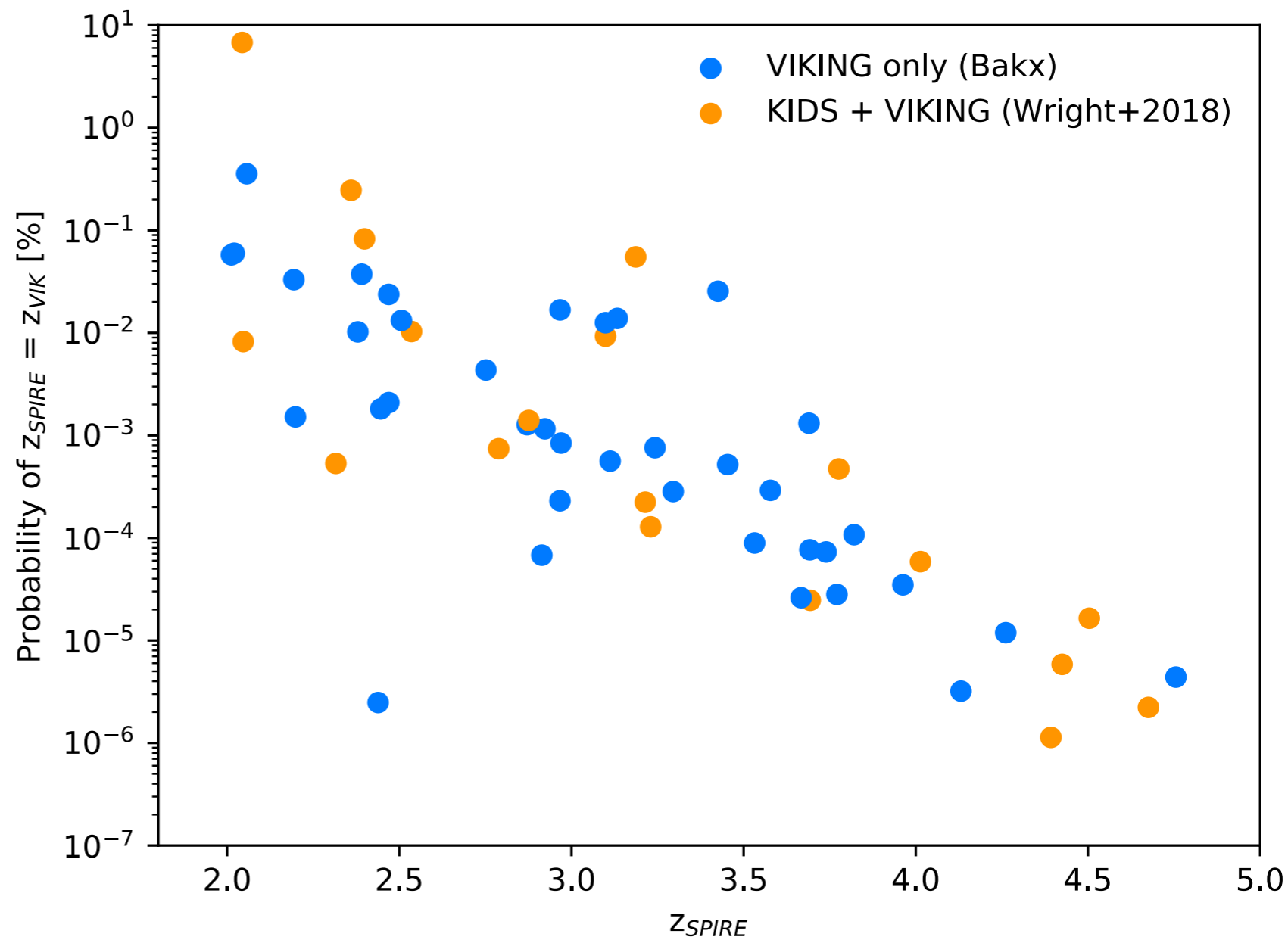
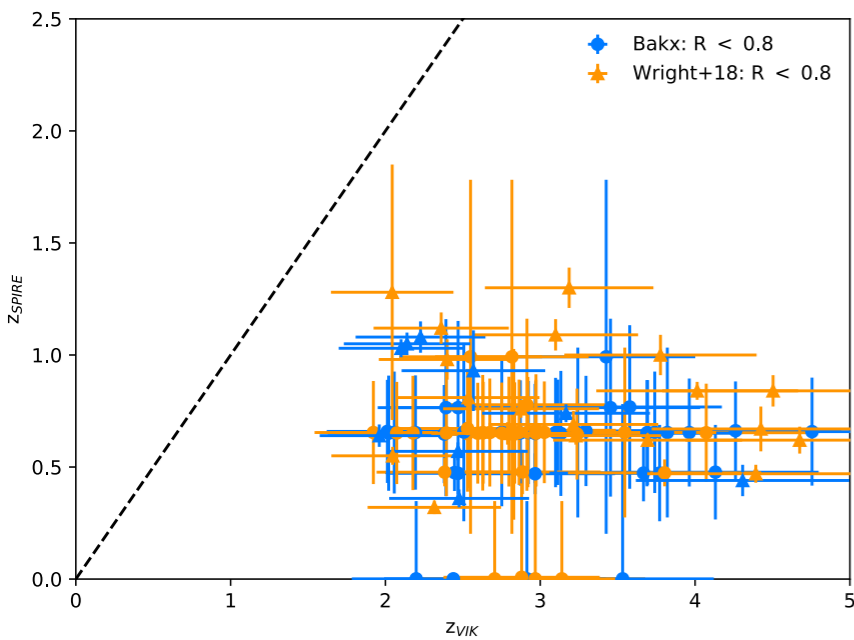
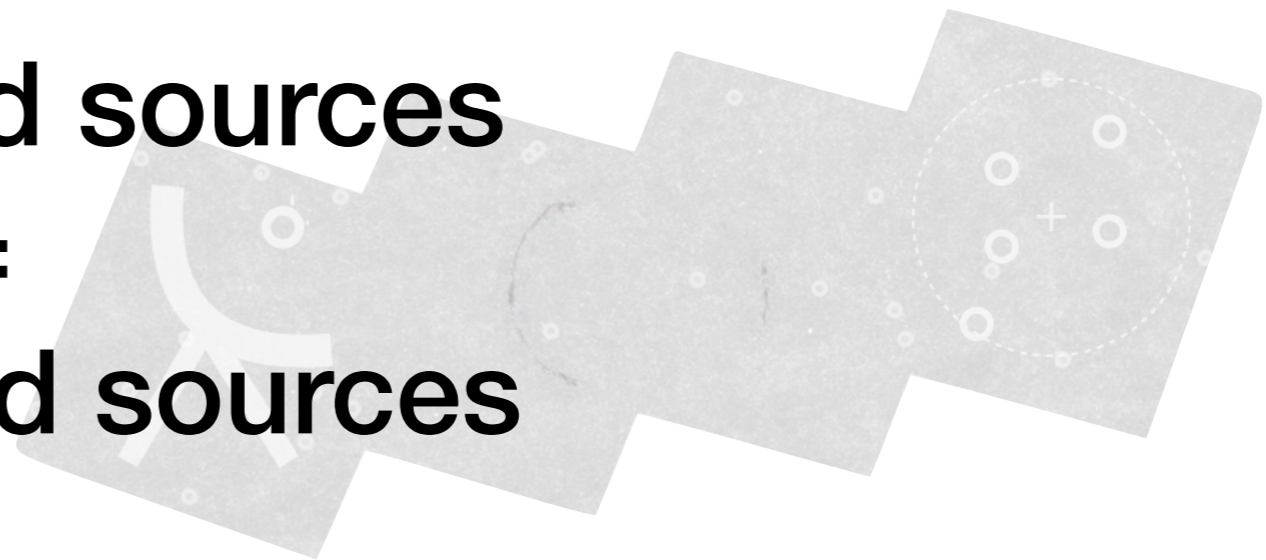
VIKING sources are extracted by minimising the residuals

Table 3. VIKING reliabilities

R	< 0.8	> 0.8	All
SGP	6	22	28
GAMA09	13	8	21
GAMA12	9	17	26
GAMA15	10	13	23
Total	38	60	98



Foreground sources ≠ Background sources



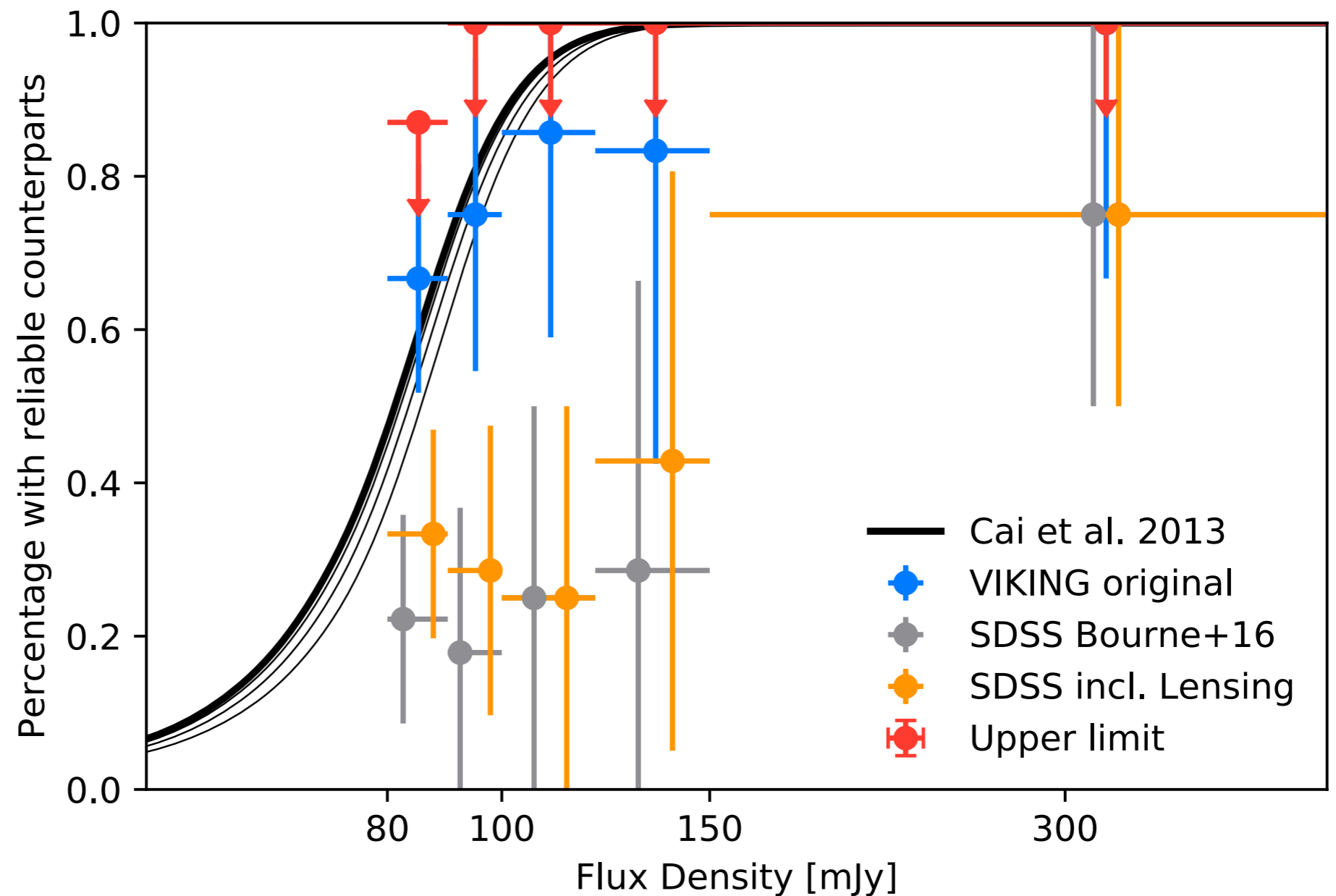


Why more is less

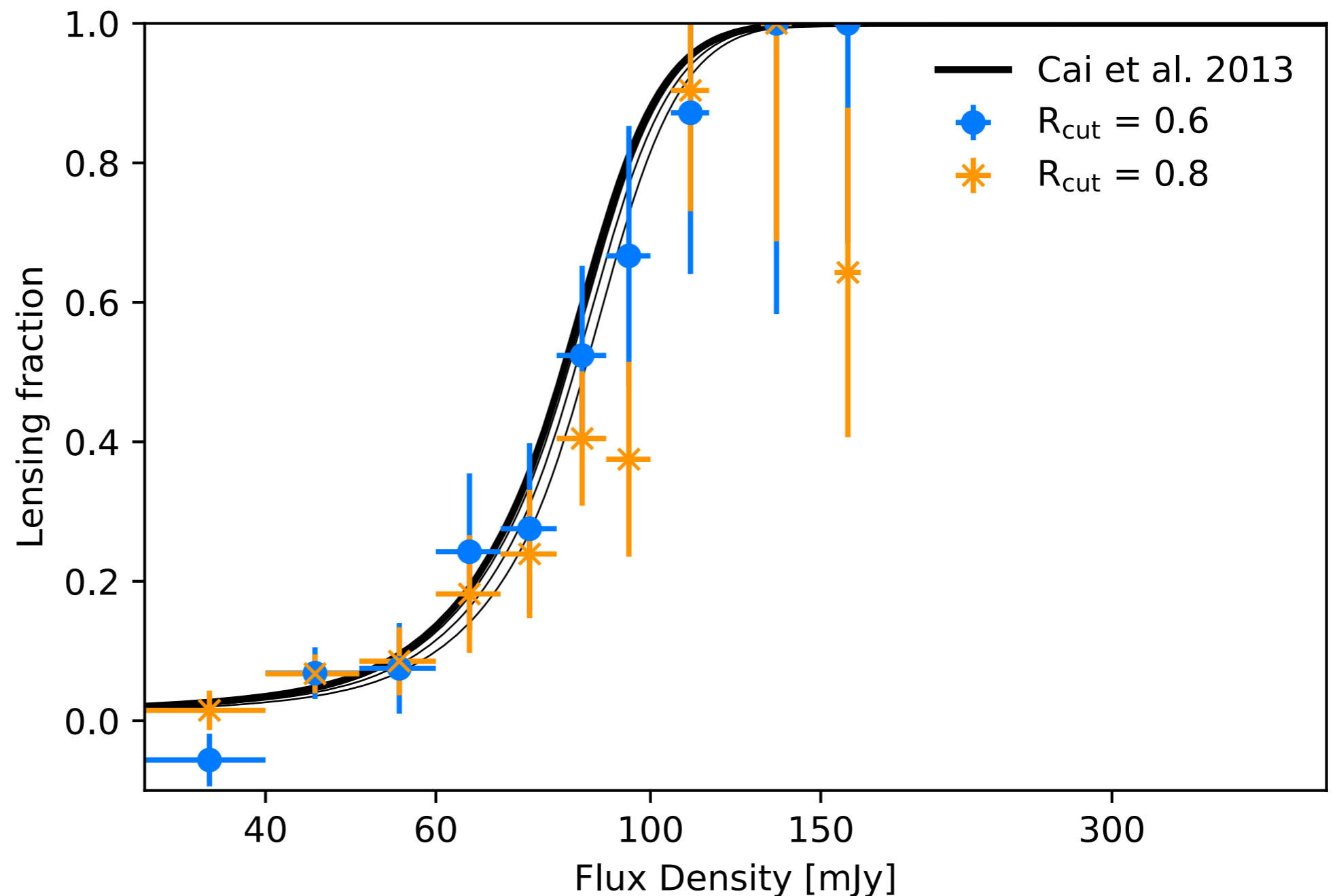
Table 4. VIKING visual inspection results

Counterpart with $R < 0.8$ because . . .	Amount
. . . i. large angular separation	\sphericalangle : 9
. . . ii. nearby, competing sources	\parallel : 14
. . . iii. close source not picked up	\otimes : 6
. . . iv. close source with $J - K_S < 0$	\leq : 2
. . . v. nothing nearby is detected	\emptyset : 7

While SDSS does not see all foreground sources, VIKING appears complete

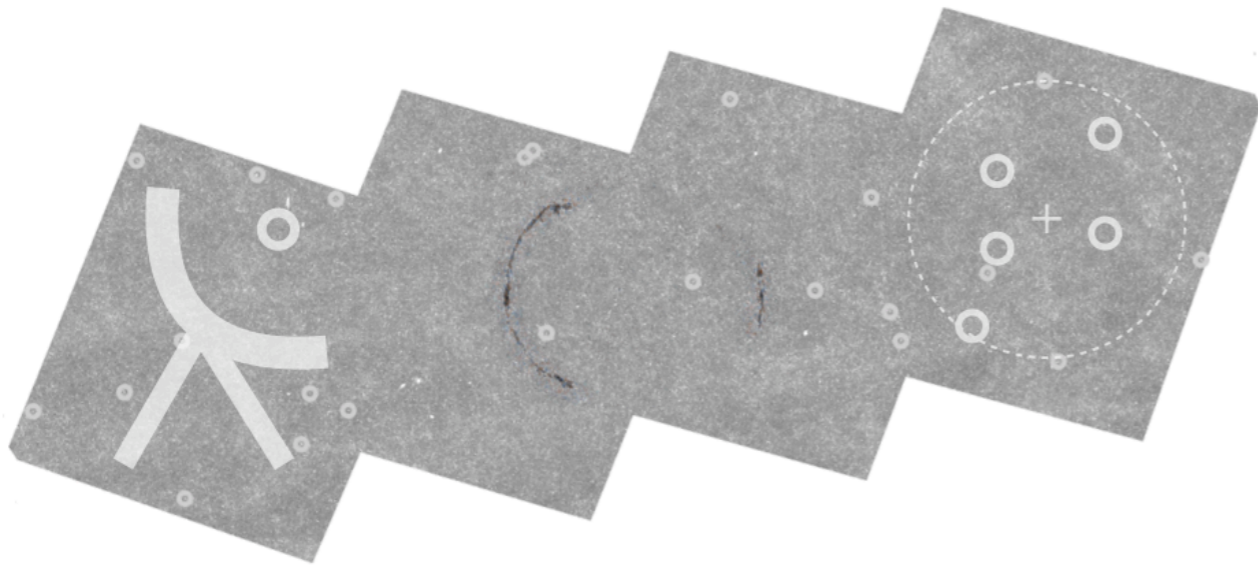


Using all Herschel sources reveals the lensing fraction



How many gravitational lenses did Herschel detect?

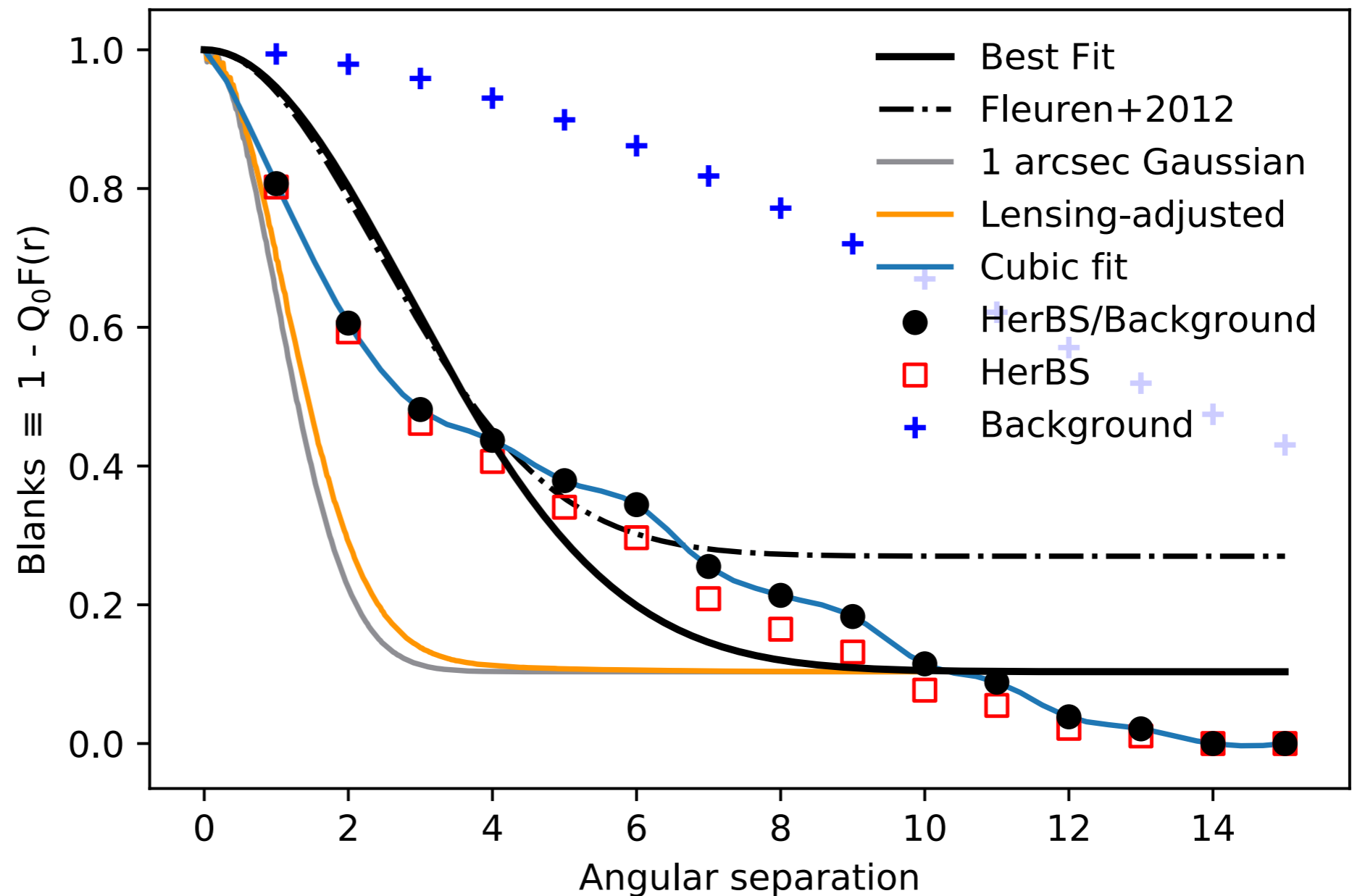
*Optical and near-infrared counterparts
to sub-mm sources*



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The sources extend out to high angular scales

Q_0 is equal to 0.8851



Recalculated angular distribution

